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Investigation of Magneto-Convection Characteristics in A Sudden Expanding Channel with Convex Surface Geometry Under Thermally Developing Flow Conditions

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Abstract

The current study presents a novelty with focusing on the magnetic field effect on a sudden expansion tube with expansion ratio, total length, and pitch length of the dimpled fin is 2.5, 1500 mm, and 3.0, respectively. The magnetizable Fe_3O_4/H_2O Ferrofluid with different nanoparticle volumetric concentrations ($\phi=1.0\%$ and 2.0%) were used as a heat transfer fluid, and magnetohydrodynamic effects were elaborately investigated in this study. The numerical analysis was conducted under laminar flow regime and the DC magnetic field ($B_0=0.03T$, $0.05T$, $0.3T$, and $0.5T$). The present study provided a comprehensive investigation, which presented the thermo-hydraulic performance of difference dimpled fins, Fe_3O_4/H_2O Ferrofluid, and magnetic field. According to the results, dimple fins showed the best increment within heat transfer enhancement techniques. The heat transfer enhancement rate of the dimple tube and Fe_3O_4/H_2O Ferrofluid were respectively acquired as 22.62% and 5.43%-6.28% ($\phi=1.0\%$ and 2.0%). When dimpled fin and Fe_3O_4/H_2O Ferrofluid were used, the increment in Performance Evaluation Criteria was calculated as 21.31% and 4.85%-9.79% ($\phi=1.0\%$ and 2.0%). Although the highest average Nusselt number was obtained at $B_0=0.5T$, the highest performance evaluation criteria were detected at $B_0=0.3T$ due to the friction factor showing an increment.

Keywords: Sudden expansion tube, Dimpled fin, DC magnetic field, Fe_3O_4/H_2O Ferrofluid, Performance Evaluation Criterion.

Nomenclature

AC alternating current

PEC performance evaluation criterion

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$\vec{B}_0$	Magnetic field intensity (T)	P	dimple distance (mm), pressure (Pa)
BF	base fluid	P/d	pitch ratio
d	dimple diameter (mm)	Re	Reynolds number
D	tube diameter (mm), dimension	SET	sudden expansion tube
DC	direct current	ST	smooth tube
DF	dimpled fin	T	temperature (K), Tesla
DT	dimpled tube	THP	thermo-hydraulic performance
$\vec{E}$	electrical field (V/m)	$\vec{V}$	velocity (m/s)
ER	expansion ratio	q''	heat flux (W/m^2)
f	frequency	Greek symbols	
ff	Darcy friction factor	ϕ	nanoparticle volumetric concentration (%)
$\vec{F}$	Lorentz force (N)	μ	dynamic viscosity ($Pa.s$), magnetic permeability (H/m)
FF	ferrofluid	Φ	dissipation energy (W/m^3)
H	dimple height (mm)	σ	electrical conductivity (S/m)
Ha	Hartmann number	Δ	difference
HTF	heat transfer fluid	ρ	density (kg/m^3)
$\vec{j}$	current density (A/m^2)	Subscripts	
k	thermal conductivity (W/mK)	b	bulk
L	longitudinal length (mm)	bf	base fluid
MF	magnetic field	in	inlet
MHD	magnetohydrodynamic	nf	nanofluid
Nu	Nusselt number	np	nanoparticle
NF	nanofluid	out	outlet
NP	nanoparticle	w	wall

1. Introduction

Global warming is one of the top issues that requires an urgent action. To reduce emission and leave a clean world for future generations 151 countries have taken considerable actions such as the “loss and damage” motto and net-zero emission by 2050 at the *COP26* summit, Glasgow Conference in 2021 [1, 2]. For this purpose, there has been significant increment in the scientific studies carried out on the use of renewable energy sources [3, 4] Most researchers have conducted a great deal of study on it. One of these studies is the heat exchanger, which is used in lots of industrial applications. The performance enhancement techniques for heat exchanger have been investigated employing passive [5] and active techniques [6] which are heat transfer improvement techniques.

For instance, rough surface, which includes dimpled fins (*DFs*), is one of the prominent passive techniques in the geometric improvement, and this phenomenon has been investigated by numerous researchers in the literature [7, 8]. Malapur et al. [9] conducted a computational analyses on five different dimpled tubes (*DT*). Researchers have aimed to investigate the effect of *DF* and compare it with the smooth tube (*ST*). According to the results, the heat transfer properties of *DT* override on *ST*, and the helical pattern of *DF* with a smaller pitch angle exhibits more heat transfer than other types of fins. Dagdevir [10] has numerically investigated the convective heat transfer (*h*) and pressure drop (ΔP)

behavior of the various *DF* parameters such as dimple diameter (*d*), dimple pitch length (*PL*), and dimple height (*H*). H_2O has been used as heat transfer fluid (*HTF*), and Reynolds number (*Re*) is considered as $Re=3000$. It was reported that the influence of *PL* is higher than the effect of *H* and *d* in terms of *h* and ΔP . Furthermore, it was found that $d=7\text{ mm}$, $PL=30\text{ mm}$, and $H=1.0\text{ mm}$ present the optimum performance regarding hydrothermal behavior. A study aimed to determine the performance of *DT* has been carried out by Kaood et al. [11]. The numerical study has been examined under $Re=3000-40000$, constant heat flux of $q''=40000\text{ W/m}^2$ and using H_2O as *HTF*. As a result, the *DT* may enhance the thermal performance of the system up to 121.4% compared to *ST*. Another study, which focused on the effect of *DF* on thermohydraulic performance (*THP*), has been conducted by Zheng et al. [12]. Researchers firstly examined the actual applicability of the elliptical *DF* to be used as a passive method and created the tube with a reasonable error rate. According to the results, Performance Evaluation Criterion (*PEC*) has reached a maximum value as 2.4 using the elliptical *DF*.

Along with the improvement of the nano technology, *NFs* have been created with the help of nanoparticles, which size is less than 100 nm [13] and dispersed in conventional *HTFs* such as H_2O , ethylene glycol, oil, etc.[14, 15]. In fact, *NFs* have been examined together with *DF* in both experimental and numerical studies in the literature. Gürsoy et al. [16] theoretically analyzed the *THP* of ferrofluid (*FF*) in a sudden expansion tube (*SET*) retrofitted with *DF*. The analyses have been performed under $100 \leq Re \leq 2000$, $q''=600\text{ W/m}^2$, and $1.0\% \leq \phi \leq 2.0\%$. The results show that the increment in *Re* affects *Nu* positively. It is also found that the flow geometry, which has an expansion ratio (*ER*) is 2.5 and a pitch ratio (*P/d*) is 3.0, at the $Re=2000$ and $\phi=2.0\%$ case provides the highest *PEC*. Ahmad et al. [17] realized a comprehensive numerical study, which has a lot of double-*DF* and *NF* configurations. The study has provided important outcomes about *DF* and *NF* effects in thermal systems. The analyses have been conducted under $Re=10000-13000$ and $q''=10\text{ kW/m}^2$. Mono and hybrid *NFs* with $1.0\% \leq \phi \leq 3.0\%$ have been used as *HTF*. The results demonstrated that double-*DFs* have enhanced the average *Nu* up to 168.2% compared to *ST*. Furthermore, it is seen that Al_2O_3-CuO/H_2O hybrid *NF* enhances the average *Nu* by 12.0% compared to Al_2O_3/H_2O .

With the addition of *NPs* to conventional *HTFs*, a few improvements are observed in the *THP*. The thermal and hydrodynamic behavior of the existing fluids might change in this way. Thus, a less increase in heat transfer coefficient and viscosity are among the results encountered by researchers [18]. To enhance thermal performance of the system, researchers have started to activate the magnetic field (*MF*) on the system as well as the *DFs*. Utilization of the *MF* is placed as one of the active heat transfer enhancement techniques [19] in the literature. Many experimental and numerical studies have been carried out on this subject, especially using Fe_3O_4 *NPs*. Recently, Gürdal et al. [20] have presented valuable studies in the literature about MagnetoHydroDynamics (*MHD*) area. A particular experimental study, in which the scope of *MHD*, has been carried out by Shahsavari et al. [21]. The researchers have utilized two active methods consisting of rotating *MF* and vibration to enhance the heat transfer rate of Fe_3O_4/H_2O *FF* flowing in a rifled tube. According to the results, vibration enhances the *PEC* up to 1.28.

Along with applying the rotating MF , PEC shows an increment of 21.32%. Halawa and Tanious [22] realized a numerical study to determine the optimum MF arrangement, which will provide the highest convective heat transfer rate in the rectangular channel using Fe_3O_4/H_2O FF . Researchers have presented detailed results about the problem. MF has reciprocally been applied on the channel at four different locations and the magnets have been placed in $N-N$, $S-N$, and $S-S$ orientations. While the MF intensity was ranged from 250 to 1000 $Gauss$, $N-N$ magnet orientation was performed with the optimum results. The results indicated that the average Nu exhibits an increment range of 16.44%–24.46% applying the MF up to 1000 $Gauss$.

When the literature review is examined, it is seen that MHD applications are made for different flow geometries and application purposes. However, the effect of DC MF on the THP of FF flowing through SET , which is modernized with DF , has not been investigated so far. This determined purpose reveals the novelty of this study. Based on this situation, the flow geometry of which the best PEC has been obtained in the study ($ER=2.5$ and $P/d=3.0$) conducted by Gürsoy et al. [16] has been used for this investigation. It has numerically been handled in this study as the fundamental flow problem, and the effect of MF on the sudden expansion geometry with FF has been examined in detail. In the study, $Re=1000$, 1500, and 2000 have been used, and FF has been prepared as $\phi=1.0\%$ and 2.0% . DC MF has been applied at $z=937.5$ mm with the intensity of $B_0=0.03$, 0.05, 0.3, and $0.5T$. The results are presented in the form of graphs and discussed in detail.

2. Geometry Description and Boundary Conditions

In this study, MHD convective heat transfer and flow characteristics of FF have been considered for the SET subjected to uniform and constant wall heat flux and DC MF . The flow chart of the problem, definitions, boundary conditions, and process stage of this analysis are given in Fig. 1. Besides, Fig. 2 shows description of the geometry and boundary conditions for investigated computational domain. The HTF enters the inlet tube of SET with $D_1=8$ mm and $L_1=375$ mm under laminar flow regime at 300 K . HTF is suddenly expanded at $z=375$ mm and starts flowing in the outlet tube with $D_2=20$ mm and $L_2=1125$ mm . Furthermore, DC MF has been applied at $z=937.5$ mm with the diversified intensities as $B_0=0.03$, 0.05, 0.3, and $0.5T$. The affected area length by MF has been considered as $L_M=100$ mm electromagnet diameter used in the experimental study carried out by Tekir et al. [23]. The geometric parameters and boundary conditions of the numerical study are summarized in Table 1.

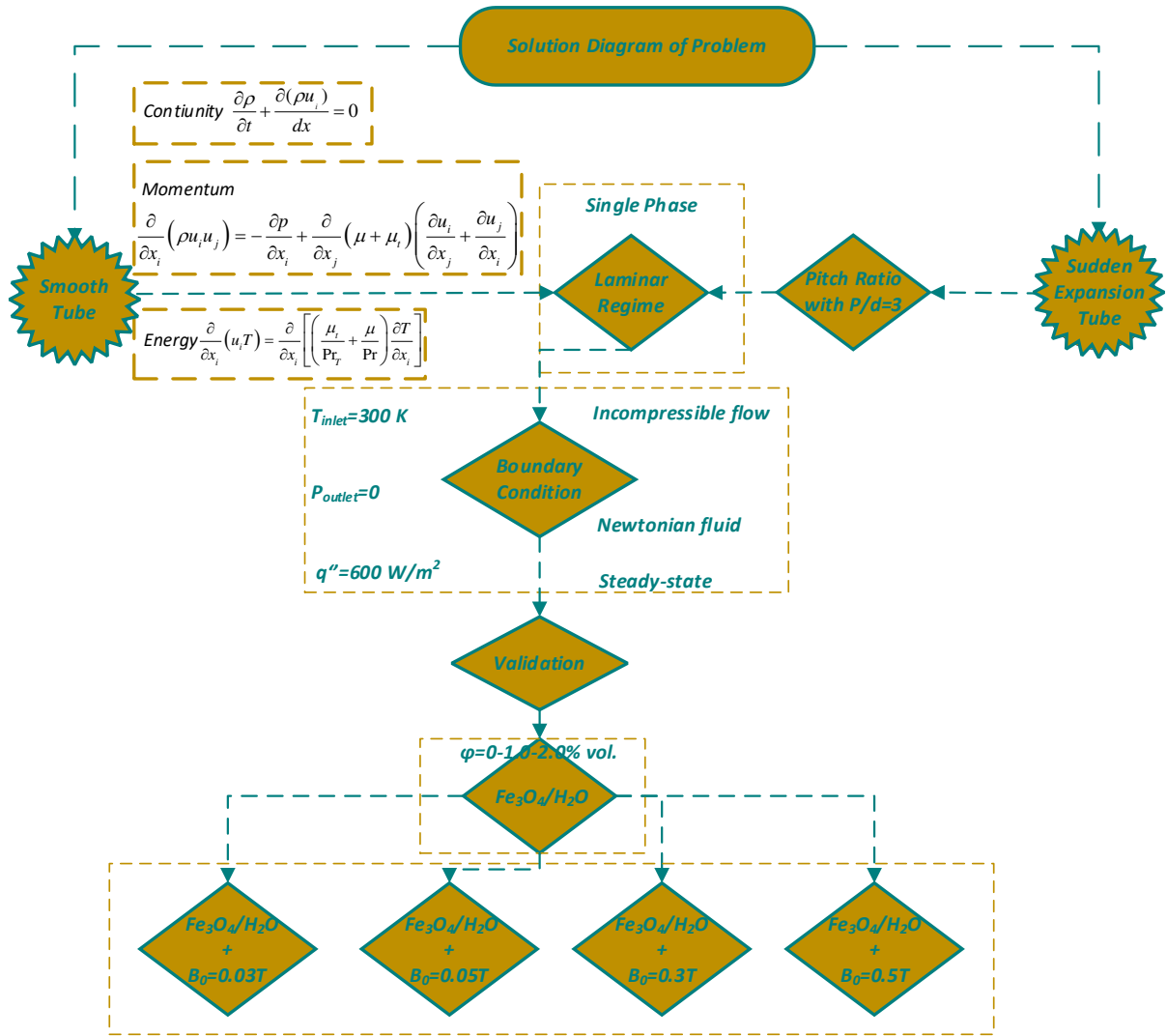
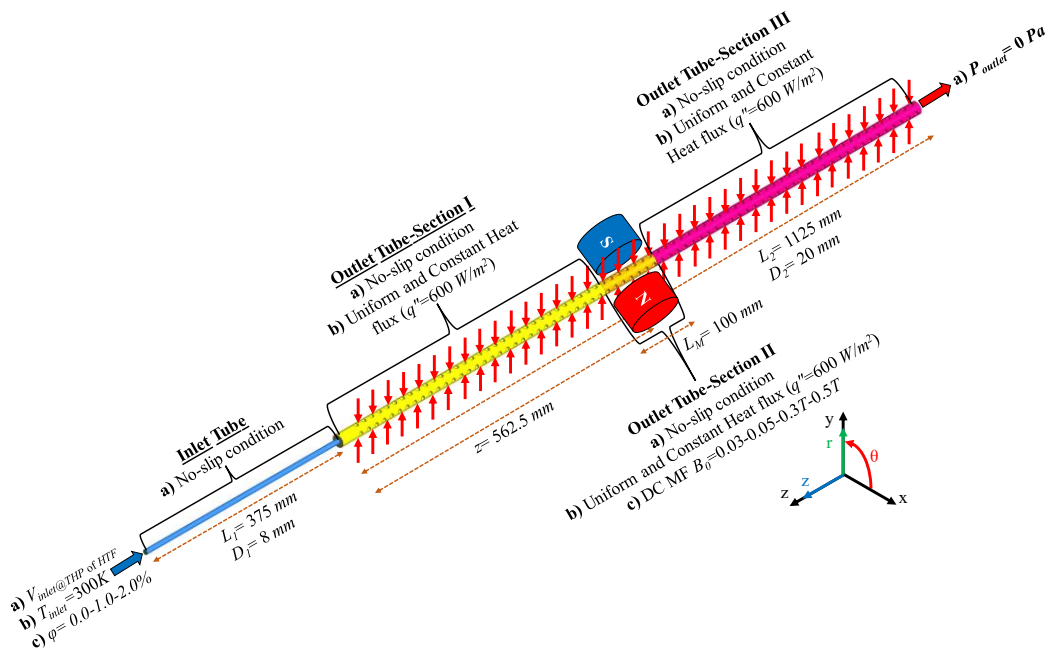


Fig. 1. Flow chart of problem solution and analysis



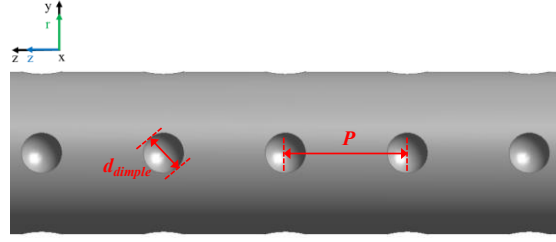


Fig. 2. Description of; (a) flow geometry and boundary conditions of the numerical study, (b) *DF* geometry.

Table 1. Geometric parameters and boundary conditions of the numerical study.

Category	Description	Parameter	Value
Geometry	Inlet tube length	L_1 (mm)	375
	Inlet tube diameter	D_1 (mm)	8
	Outlet tube length	L_2 (mm)	1125
	Outlet tube diameter	D_2 (mm)	20
	<i>DF</i> diameter	d_{dimple} (mm)	5
	Pitch length	P (mm)	15
	Location of <i>MF</i>	z (mm)	562.5
	Effect area length of <i>MF</i>	L_M (mm)	100
Boundary conditions	Inlet temperature	T_{inlet} (K)	300
	*Inlet velocity	V_{inlet} (m/s)	@ <i>THP</i> of <i>HTF</i>
	Outlet pressure	P_{outlet} (Pa)	0
	Heat flux	q'' (W/m ²)	600
	<i>FF</i> volumetric concentration	ϕ (%)	0.0-1.0-2.0
	<i>DC MF</i> intensity	B_0 (T)	0.03-0.05-0.3-0.5
	Hartmann number	Ha (-)	0.32-0.52-3.18-5.30

* Since Re is constant, the inlet velocity varies according to the *THP* of the *HTF*.

3. Mathematical Modeling and Solution Procedure

In this section, mathematical formulas, thermophysical properties of *HTFs*, and solution procedure are given for solving numerical studies with the properties defined in Section 2.

3.1. Governing equations

The fluid data has been solved via Finite Volume Method. With this approach, the continuity equation is presented in Eq. (1) [24].

$$\frac{\partial \rho}{\partial t} + \frac{1}{r} \frac{\partial}{\partial r} (r \rho V_r) + \frac{1}{r} \frac{\partial (\rho V_\theta)}{\partial \theta} + \frac{\partial (\rho V_z)}{\partial z} = 0 \quad (1)$$

Any change is not seen in the continuity equation with applying the *MF* [25]. The momentum equation, which analyzed the movement of *HTF* and including the Lorentz force, is given in Eq. (2-4) as component [26, 27].

r-component of Momentum equation:

$$\rho \left(V_r \frac{\partial V_r}{\partial r} + \frac{V_\theta}{r} \frac{\partial V_r}{\partial \theta} - \frac{V_\theta^2}{r} + V_z \frac{\partial V_r}{\partial z} \right) = -\frac{\partial P}{\partial r} + \rho g_r + \mu \left(\frac{\partial^2 V_r}{\partial r^2} + \frac{1}{r} \frac{\partial V_r}{\partial r} - \frac{V_r}{r^2} + \frac{1}{r^2} \frac{\partial^2 V_r}{\partial \theta^2} - \frac{2}{r^2} \frac{\partial^2 V_\theta}{\partial \theta} + \frac{\partial^2 V_r}{\partial z^2} \right) + q(E_0 + V_r B_0) B_0 \quad (2)$$

θ -component of Momentum equation:

$$\rho \left(V_r \frac{\partial V_\theta}{\partial r} + \frac{V_\theta}{r} \frac{\partial V_\theta}{\partial \theta} - \frac{V_r V_\theta}{r} + V_z \frac{\partial V_\theta}{\partial z} \right) = -\frac{1}{r} \frac{\partial P}{\partial \theta} + \rho g_\theta + \mu \left(\frac{\partial^2 V_\theta}{\partial r^2} + \frac{1}{r} \frac{\partial V_\theta}{\partial r} - \frac{V_\theta}{r^2} + \frac{1}{r^2} \frac{\partial^2 V_\theta}{\partial \theta^2} + \frac{2}{r^2} \frac{\partial^2 V_r}{\partial \theta} + \frac{\partial^2 V_\theta}{\partial z^2} \right) + q(E_0 + V_\theta B_0) B_0 \quad (3)$$

z -component of Momentum equation:

$$\rho \left(V_r \frac{\partial V_z}{\partial r} + \frac{V_\theta}{r} \frac{\partial V_z}{\partial \theta} + V_z \frac{\partial V_z}{\partial z} \right) = -\frac{\partial P}{\partial z} + \rho g_z + \mu \left(\frac{\partial^2 V_z}{\partial r^2} + \frac{1}{r} \frac{\partial V_z}{\partial r} + \frac{1}{r^2} \frac{\partial^2 V_z}{\partial \theta^2} + \frac{\partial^2 V_z}{\partial z^2} \right) + q(E_0 + V_z B_0) B_0 \quad (4)$$

Lorenz Force acting in the counter effect on flow [28] is obtained as follows [29].

$$\vec{F} = \vec{j} \times \vec{B}_0 \quad (5)$$

While the $\vec{j}$ (A/m^2) symbolizes the current density [29] given in Eq. (6) and obtained from Ohm's law.

$\vec{B}_0$ (T) denotes MF intensity derived from Maxwell's equations.

$$\vec{j} = \sigma (\vec{E} + \vec{V} \times \vec{B}_0) \quad (6)$$

where σ (S/m), $\vec{E}$ (V/m), and $\vec{V}$ (m/s) describe the electrical conductivity of FF , electric field, and HTF velocity, respectively. The Lorentz force, also known as the magnetic field force, is solved with the Navier-Stokes equations. In this scope, the MHD equation [30, 31] defined by Ohm's law and Maxwell's Equations and given in Eq. (7) is solved to be able to calculate the MHD effect.

$$(\vec{V} \cdot \nabla) \vec{B}_0 = \frac{1}{\mu\sigma} \nabla^2 \vec{B}_0 + (\vec{B}_0 \cdot \nabla) \vec{V} \quad (7)$$

The energy equation used for single-phase numerical solutions is given in Eq. (8) [32]. As in the momentum equation, the heat is generated as a result of applying a MF and passing an electric current through conductive materials should also be included in the energy equation. This effect, which is included in the literature as the term Joule Heating [33], is expressed by Eq. (9) and added to the right side of Eq. (11) in scope of MHD .

$$\rho c_v \left(V_r \frac{\partial T}{\partial r} + \frac{V_\theta}{r} \frac{\partial T}{\partial \theta} + V_z \frac{\partial T}{\partial z} + \frac{\partial T}{\partial t} \right) = k \left(\frac{\partial^2 T}{\partial r^2} + \frac{1}{r} \frac{\partial T}{\partial r} + \frac{1}{r^2} \frac{\partial^2 T}{\partial \theta^2} + \frac{\partial^2 T}{\partial z^2} \right) + \mu \Phi \quad (8)$$

$$Q = \frac{1}{\sigma} \vec{j} \cdot \vec{j} \quad (9)$$

where Φ (W/m^3) is the dissipation energy, which indicates the consumed power against viscous forces.

3.2. Thermophysical properties of Fe_3O_4/H_2O Ferrofluid and data reduction

In this study, Fe_3O_4 NPs dispersed with $\phi=1.0\%$ and 2.0% in H_2O , and pure H_2O were used as HTF. The basic thermophysical properties of H_2O and Fe_3O_4 NP at $T=300$ K are given in Table 2. To calculate the thermophysical properties of FF, well-known correlations in literature have been used. These thermo-physical properties calculation equations and data reduction equations to be used to evaluate the numerical analysis results are given in Table 3.

Table 2. Thermophysical properties of H_2O and Fe_3O_4 NP [16, 34].

Fluid/Particle	Density, ρ (kg/m^3)	Thermal conductivity, k (W/mK)	Dynamic viscosity, μ_{HTF} , (Pa.s)	Specific heat, c_p (J/kgK)	Magnetic permeability, μ (H/m)	Electrical conductivity, σ , (S/m)
H_2O	998	0.600	1.003×10^{-3}	4182	$1.25e^{-6}$	0.05
Fe_3O_4	5180	80.4	-	670	$8.80e^{-6}$	25000

Table 3. Data reduction equations used in the study.

Parameter	Equation	Reference	Equation number
Density [kg/m^3]	$\rho_{nf} = (1 - \phi)\rho_{bf} + \phi\rho_{np}$	[35]	(10)
Thermal conductivity [W/mK]	$\frac{k_{nf}}{k_{bf}} = \frac{k_{np} + 2k_{bf} - 2\phi(k_{bf} - k_{np})}{k_{np} + 2k_{bf} + \phi(k_{bf} - k_{np})}$	[36]	(11)
Dynamic viscosity [Pa.s]	$\frac{\mu_{nf}}{\mu_{bf}} = (1 + 7.3\phi + 123\phi^2)$	[37]	(12)
Specific heat [J/kgK]	$c_{p_{nf}} = \frac{(1 - \phi)(\rho c_p)_{bf} + \phi(\rho c_p)_{np}}{\rho_{nf}}$	[38]	(13)
Reynolds number [-]	$Re = \frac{\rho V D}{\mu_{HTF}}$	[39]	(14)
Heat convection coefficient [W/m^2K]	$h = \frac{q''}{(T_w - T_b)}$	[39]	(15)
Bulk temperature [K]	$T_b = \frac{T_{in} + T_{out}}{2}$	[39]	(16)
Nusselt number [-]	$Nu = \frac{hD}{k}$	[40]	(17)
Darcy friction factor [-]	$ff = \frac{\Delta P}{\left(\frac{L}{D}\right)\left(\frac{\rho V^2}{2}\right)}$	[41]	(18)
Performance Evaluation Criterion [-]	$PEC = \frac{\left(\frac{Nu_{enhanced}}{Nu_{base}}\right)}{\left(\frac{ff_{enhanced}}{ff_{base}}\right)^{1/3}}$	[42]	(19)

3.3. Solution method

The iterative solutions have been conducted via ANSYS Fluent 2020 R2 software. Single-phase fluid properties have been accepted for the analyses. Whereas the no-slip condition has been assumed for all tube walls, the heat flux of $q''=600 \text{ W/m}^2$ has been just applied to the outlet tube. Analyses have been conducted using the steady-state flow condition. Pressure-based solver has been used for the solutions. Also, absolute velocity formulation has been assumed. The SIMPLE algorithm has been preferred as a pressure-velocity coupling method due to being faster than other solvers. As the Spatial Discretization, Squares Cell Based, Second Order, and Second Order Upwind methods have been used as the discrimination of the governing equations.

4. Mesh Independency Study and Validation

Since the element number of a mesh directly affects the solution time, the mesh independency study must be performed for the fluid domain to obtain the optimum element number [43]. For this purpose, the analysis has been carried out under $Re=1000$ using H_2O as the *HTF*. The fluid domain has meshed using global and local mesh settings to reach the suitable mesh quality. After that, mesh independency analyses have been conducted using variable mesh values. The Nu and ff results obtained from various mesh element numbers are presented in Fig. 3. It is seen that the results exhibited stability after the 2499684 element numbers. The mesh settings at this point have been approved as the base mesh settings for all fluid domains. The obtained mesh structures are presented in Fig. 4.

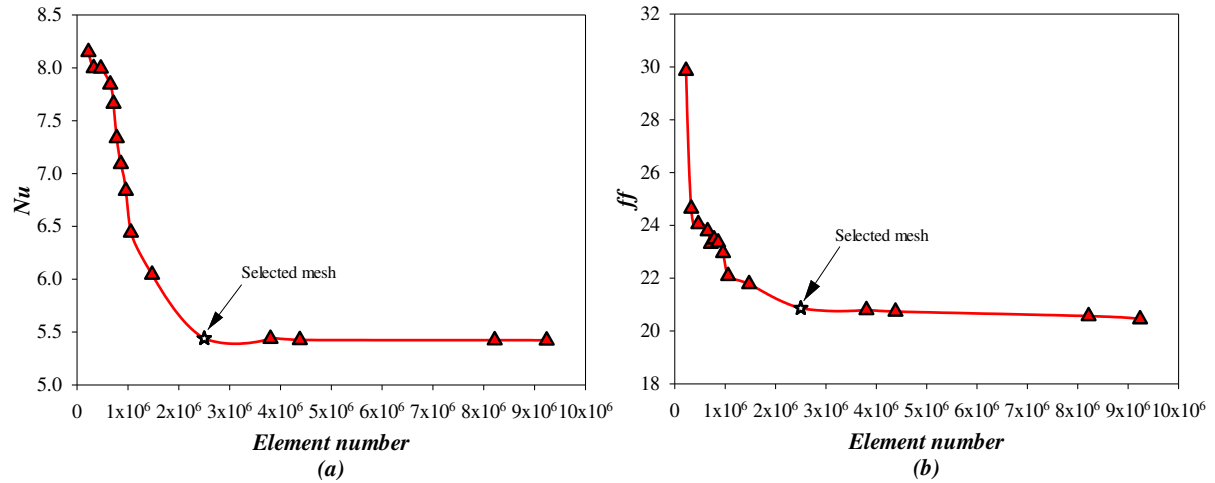


Fig. 3. Mesh independency results for $Re=1000$ using H_2O ; (a) Nu , (b) ff .

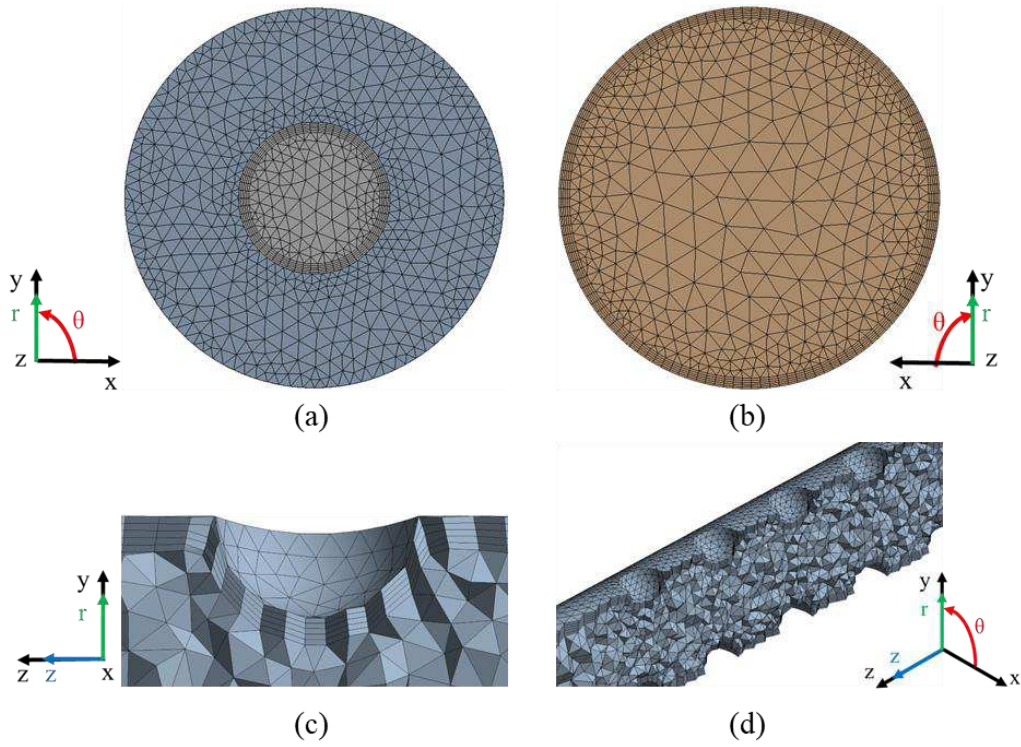


Fig. 4. Base mesh structures at; (a) inlet section, (b) outlet section, (c) *DF* side, and (d) longitudinal view.

To demonstrate the validity of the analyses, the results have been compared with previously published studies in the literature. For this purpose, the fluid domain without *DF* has been formed and results have been obtained at $Re=290$ using H_2O as *HTF*. As a result of this, the numerical results have been compared with Ref. [44]. The validation has been carried out with the help of the velocity profile given in Fig. 5 at the sudden expansion point ($z=375\text{ mm}$). It is concluded that there is a good agreement between the present study and the data obtained from the literature.

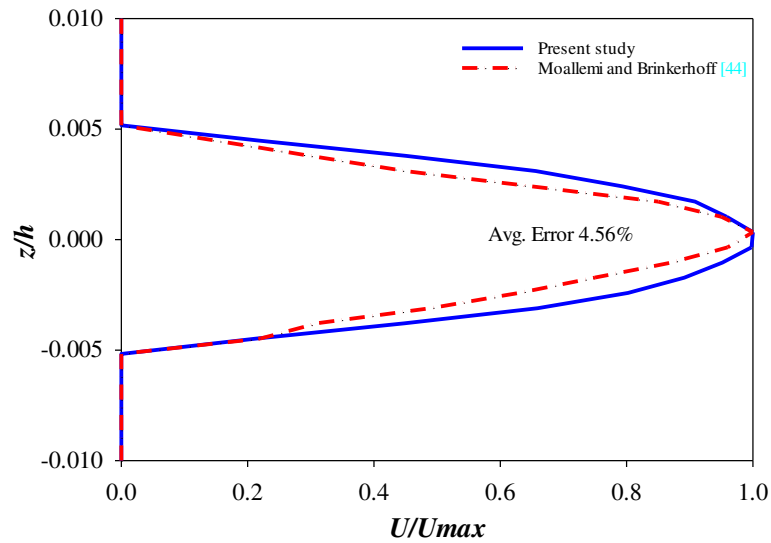


Fig. 5. Validation of the results with literature using velocity profile at $z=375\text{ mm}$.

5. Results and Discussion

5.1. Effect of dimple fin and ferrofluid on heat transfer and flow characteristics

The effect of DF and Fe_3O_4/H_2O FF on THP has comprehensively been given in Fig. 6. Generally, the average Nu and average ff exhibit an increment and decrement as the increment of Re , respectively. Moreover, the average Nu and ff show a rising up in the case of using DT compared to ST . For example, the average Nu presents an enhancement of 22.62% whereas an increase of 3.28% is realized for the average ff at $Re=2000$. When investigating the effect of Fe_3O_4/H_2O FF on THP , the average Nu shows an augmentation of 5.43% and 6.27% for $\phi=1.0\%$ and 2.0% , respectively compared to H_2O at $Re=2000$. Furthermore, a drastic soaring is realized in ff as 3.16% and 3.21% for $\phi=1.0\%$ and 2.0% at $Re=2000$, respectively. It is concluded that using DT is more effective than using Fe_3O_4/H_2O FF in terms of heat transfer enhancement, and this result is supported in a study published by Pourfattah et al. [45]. In the case of using DT and 2.0% Fe_3O_4/H_2O FF , 30.31% raise is observed for average Nu at $Re=2000$ while an boost of 6.60% is occurred for average ff .

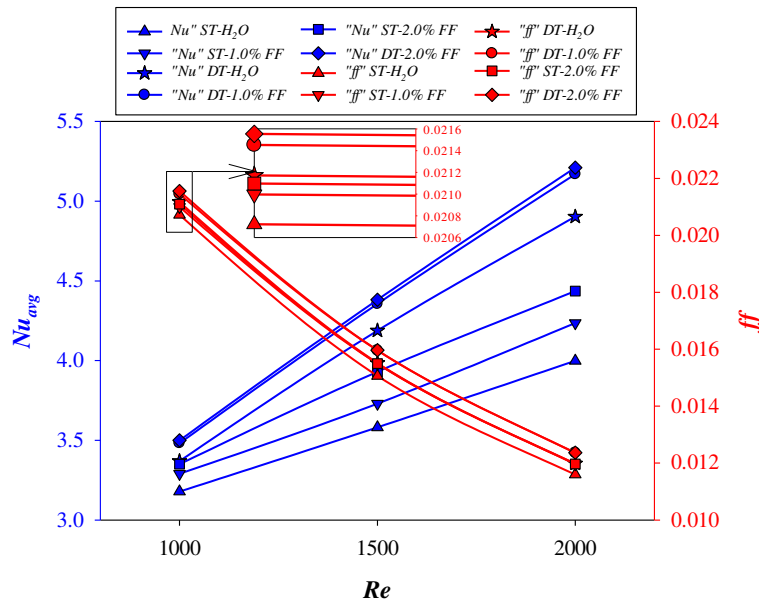


Fig. 6. Variation of average Nu and ff with Re under DT and FF effect.

It has already been mentioned that the presence of DF is more efficient than the use of NF for enhancing heat transfer. To demonstrate the heat transfer and flow characteristics mechanism of DT , a visual description is presented in Fig. 7 (a-c). In Fig. 7 (a), the streamlines and local Nu distribution are shown flowing through the tube. While the HTF flows in the DF at $Re=2000$, HTF impinges the upstream side of the DF , and flow is interrupted. The velocity profile is approached to the center of the tube due to the effect of this interruption, and flow separation is formed on the upstream side of DF [46]. This phenomenon positively affects the flow in terms of THP by thinning the velocity boundary layer. As a result, the pressure and inertia forces are more dominant than the viscous force, and the thermal boundary layer thickness becomes thinner [47]. Thus, the THP of the SET exhibits an enhancement as

the decrement of the field synergy angle (α) [48]. As the *HTF* flows over the protrusion section of the *DF*, an increase in *HTF*'s velocity takes place due to narrower cross-section, and then the *HTF* spreads over a larger volume. Due to this spread, secondary flow occurs, which prevents the convection of heat flux applied downstream of the *DF* to the *HTF*. Furthermore, Fig. 7 (b) and (c) show the comparison of local Nu distribution on outlet tubes for *ST* and *DT*. As can be seen from the figures, *DT* provides superiority over *ST* in terms of convective heat transfer thanks to the enhancement in local Nu values. Fig. 7 (c) explicitly presents the difference of top and bottom walls in terms of surface Nu distribution. According to the contours, the top wall realizes more heat transfer than the bottom wall for judging by the entire tube and this result presents similarity with the data in Ref. [49].

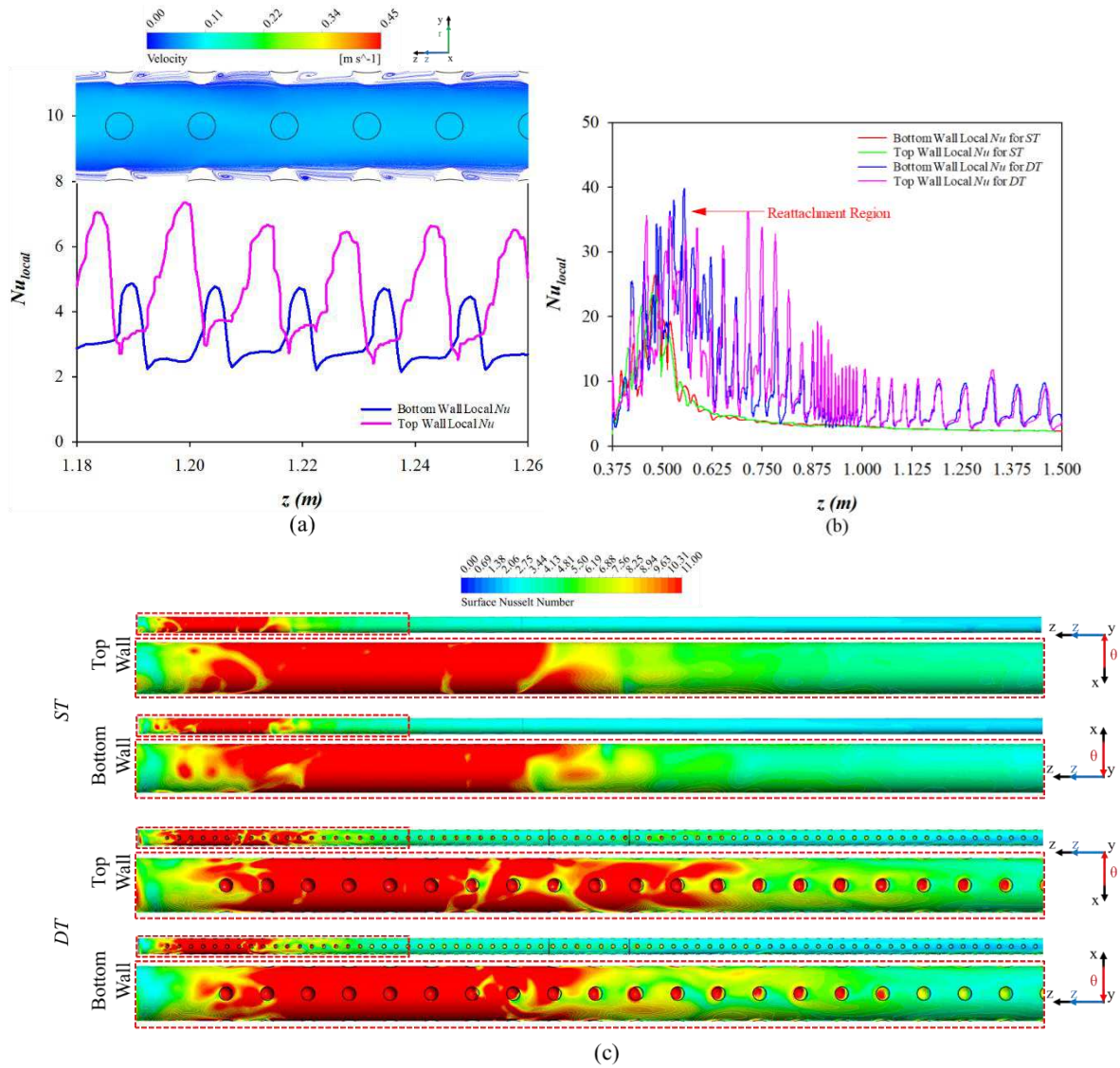


Fig. 7. Effect of *DF* on *THP* at $Re=2000$; (a) interaction of heat transfer and flow characteristics in *DT*, (b) comparison to Nu_{local} in *ST* and *DT* as a trend (c) comparison to Nu_{local} distribution in *ST* and *DT*.

Investigation of the *PEC* presents the applicability and feasibility of the designed thermal system. Within the scope of this concept, the *PEC* results have been presented in Fig. 8 to exhibit the *THP*. The trends show that obtained thermal performance using the *DF* and *FF* come to the forefront compared to the adverse effect of hydraulics. Besides, it is seen that the using *DF* dominates the using *Fe₃O₄/H₂O FF* in terms of *THP*. When the evaluation has made for *DF* alone, it was determined that *PEC* rises by 21.31% at *Re*=2000. When the evaluation has made for *Fe₃O₄/H₂O FF* alone, it was determined that *PEC* soars by 4.85% and 9.79% at *Re*=2000 for $\phi=1.0\%$ and 2.0% , respectively. In the case of the use of *DF* and *FF* together, *PEC* exhibits an increment of 26.58% and 27.56% at *Re*=2000 for $\phi=1.0\%$ and 2.0% , respectively.

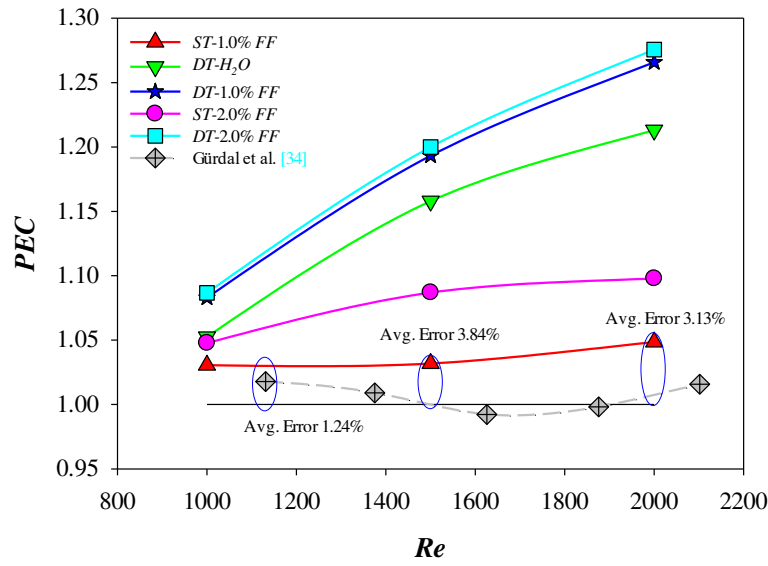


Fig. 8. Variation of *PEC* with *Re* under *DT* and *FF* effect.

The increment in convective heat transfer that occurs with the use of *Fe₃O₄/H₂O FF* has been attributed to the Brownian motion and Thermophoresis phenomena, which are also referred to as slip mechanisms by many researchers [50, 51]. The Brownian motion defines as the random motion of *NPs* and collides of these *NPs* with each other. As a result of this interaction, heat is transferred from one *NP* to another. While the *NP* flows in the *HTF*, heat transfer realizes in two different ways. The first phenomenon is called direct contribution, which can explain by the heat transfer among the *NPs*. In contrast, the second phenomenon is called indirect contribution (micro-convection), which is realized between *NP* and *HTF* that surrounds the *NP* [52]. The Brownian motion disrupts the thermal boundary layer, and this phenomenon contributes to enhancing the convective heat transfer performance of the system [53]. Another effect is the Thermophoresis phenomenon (also known as the Soret effect [54]), which has been studied by many researchers and is claimed to be worth investigating [55, 56]. Thermophoresis can be defined as the time-averaged force formed by the Brownian motion of the *NPs* in the *HTF* under the influence of temperature gradient [57]. With the effect of this force, the particles in the hot region of the

flow area tend to flow toward the cold regions. Because the Thermophoretic force, which is proportional to the temperature gradient, has higher values in the higher temperature gradient [58].

5.2. Effect of magnetic field on heat transfer and flow characteristic

The application of the MF in a SET put forward the novelty of this study. Within this scope, different DC MF intensities ($B_0=0.03T$, $0.05T$, $0.3T$, and $0.5T$) have been applied on the outlet tube wall at $z=937.5$ mm. The THP behavior of DT in both presence and absence of MF is given in Fig. 9. The results exhibit a closeness to each other. However, it can be mentioned that as the intensity of MF grows, the average Nu and average ff show an increase. The highest average Nu has been obtained as 5.28 for the case of $B_0=0.5T$ and $Re=2000$ using $\varphi=2.0\%$ Fe_3O_4 FF . When a comparison is carried out between DC MF intensities and the absence of MF , the average Nu performs an increment of 0.42%, 0.74%, 1.22%, and 1.42% for $B_0=0.03T$, $0.05T$, $0.3T$, and $0.5T$, respectively. On the other hand, the average ff tends to decrease with the increment of Re , gradually. Compared to the absence of MF , the average ff shows an increment of 0.30%, 0.50%, 1.30%, and 2.50% for $B_0=0.03T$, $0.05T$, $0.3T$, and $0.5T$, respectively.

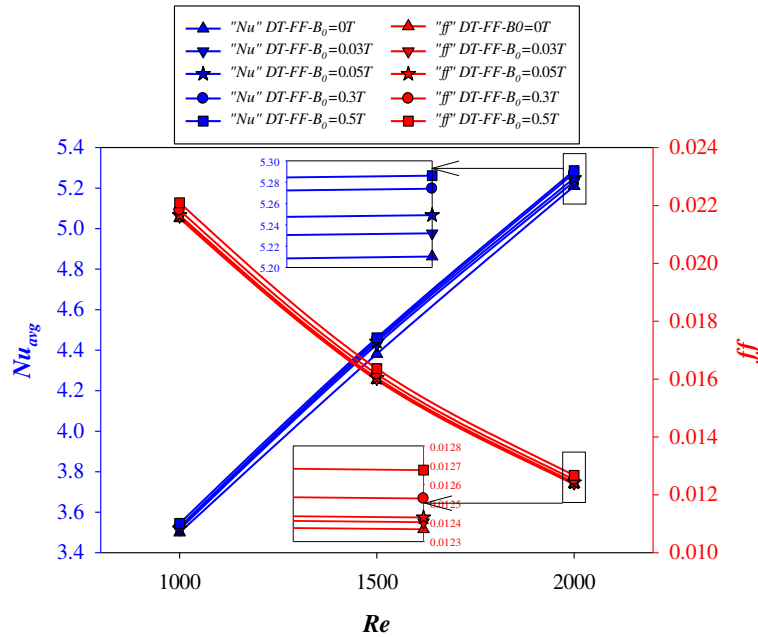


Fig. 9. Variation of average Nu and ff with Re under different DC MF intensities.

Many factors can explain the variation in the THP of the system with the application of MF . The one of the most important effects is the Lorentz force, which occurs due to the electrical conductivity of the HTF . Based on the MHD , when an external MF is applied to the magnetizable NPs , creates an effect called the Lorentz force between the fluid and the MF source [59]. The Lorentz force acts HTF flow at the opposite direction, which causes occurrence of vortex in the MF applied region [34, 60]. Another factor affecting THP is the magnetophoresis transport mechanism [61] formed by Fe_3O_4 NP acting in MF . Magnetophoresis is a heterogeneous behavior from quasi-homogeneous behavior when

magnetizable NPs such as Fe_3O_4 NP are attracted to the tube's wall under the influence of an MF . The NPs are attracted to the tube's wall and disperse the boundary layers there leading an increase in heat transfer rate.

The effect of DC MF on PEC is presented in Fig. 10 using Fe_3O_4/H_2O FF with $\phi=2.0\%$. According to the results, the PEC shows an increment up to $B_0=0.3T$. When the Fe_3O_4/H_2O FF is subjected to $B_0=0.5T$ DC MF , the PEC exhibits a decrement. A similar result has been acquired by Ghofrani et al. [62] and Yarahmadi et al. [63]. When a detailed investigation carries out on the results, it is obtained that the PEC of Fe_3O_4/H_2O FF flowing in DT performs an increment of 27.97%, 28.30%, 28.57%, and 28.31% with exposed to $B_0=0.03T$, 0.05T, 0.3T, and 0.5T DC MF , respectively.

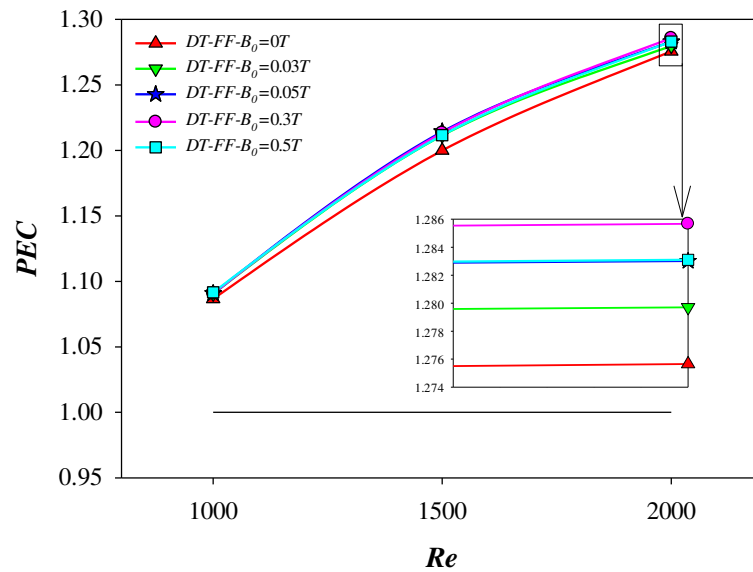


Fig. 10. Variation of PEC with Re under different DC MFs intensities.

To demonstrate the DC MF effect on heat transfer, the surface Nu distribution at MF applied surface is presented in Fig. 12 for $B_0=0T$ and 0.3T DC MFs at $\phi=2.0\%$ and $Re=2000$. The surface Nu distributions are demonstrated for x and $-x$ direction surfaces. The distributions show that MF has a positive effect on heat transfer not only on the MF applied surface but also after this region. The main reason underlying this result is based on the effect of MF on flow motion.

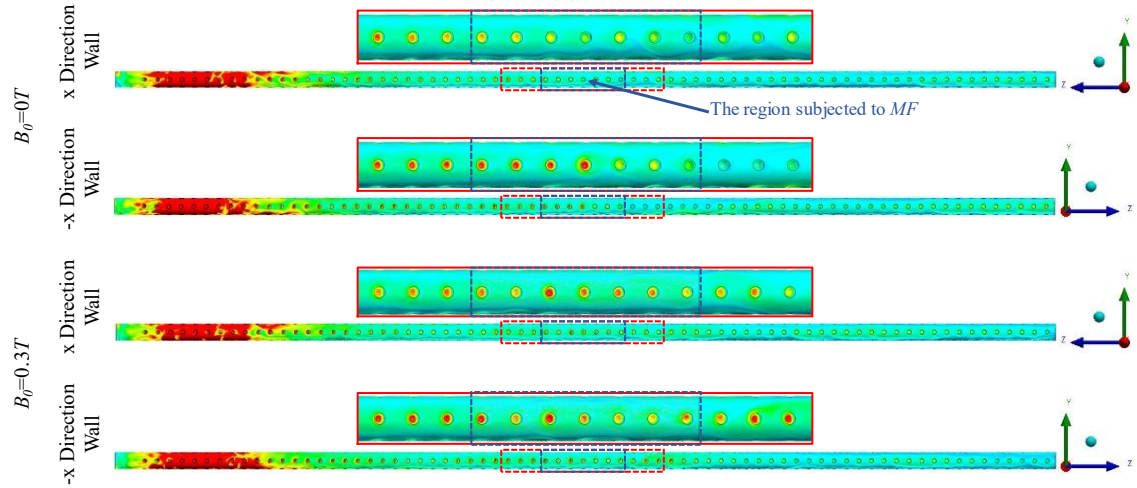


Fig. 12. Exhibiting the surface Nu distribution.

The effect of *DC MF* on temperature gradient and vorticity formation at $Re=2000$ and $z=927.5$ mm is presented in Fig. 13. It can be seen that along with increments of the *DC MF* intensity, the temperature gradient becomes a more uniform situation shown in Fig 13 (a). However, the same explanation cannot be made for the vorticity formation given in Fig. 13 (b). As the *DC MF* intensity increases, no visible change in vorticity formation is observed.

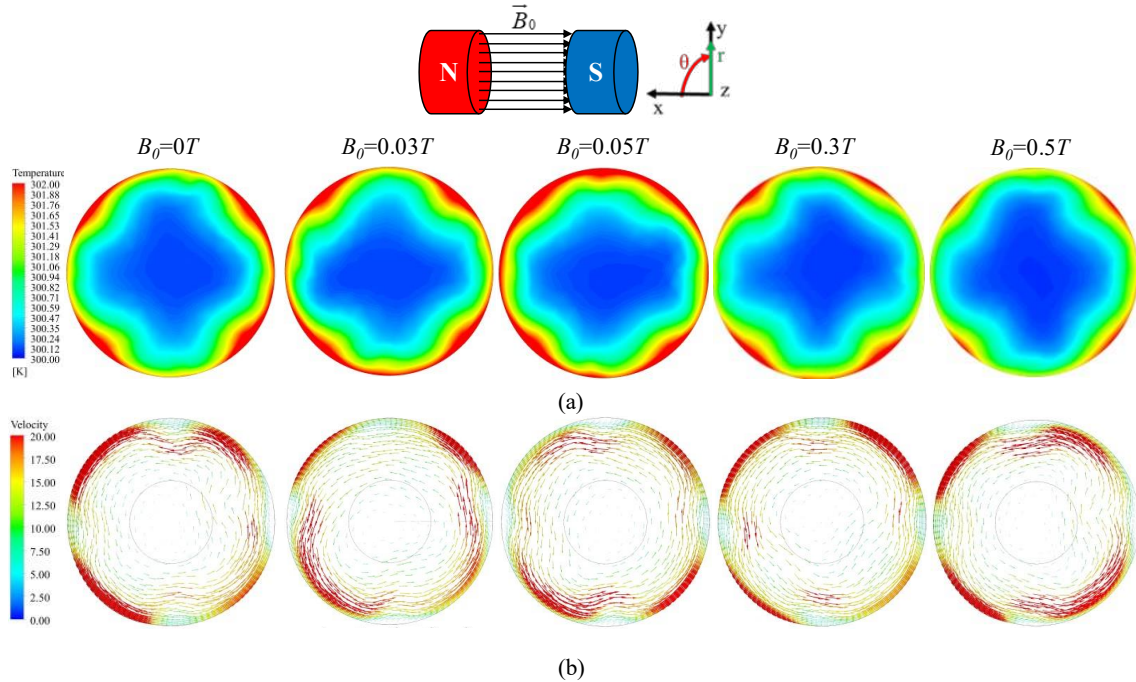


Fig. 13. *DC MF* effect on (a) temperature gradient and (b) vorticity formation.

6. Conclusions

In this study, the influence of the compound heat transfer enhancement techniques, which include *DF*, *NF*, and *MF* is detailly investigated in *SET* to determine the *THP* effect. The result of average Nu ,

local Nu , average ff , local ff , average velocity, local velocity, and PEC are presented with graphs while surface Nu distribution on DT and $DC MF$ applied regions, temperature gradient, and vorticity formation at $DC MF$ region are tackled, in detail. The following remarks can be summarized below.

- The average Nu and ff show an increment of 22.62% and 3.28% in DT compared to ST using H_2O at $Re=2000$.
- Using $Fe_3O_4/H_2O FF$ shows an enhancement of 5.43% and 6.27% in average Nu for $\phi=1.0\%$ and 2.0%, respectively, compared to H_2O in the same conditions. Besides, $Fe_3O_4/H_2O FF$ increments the average ff by 3.16% and 6.27% compared to H_2O , respectively.
- The use of DF provides a 21.31% increment in PEC , while the use of $Fe_3O_4/H_2O FF$ with $\phi=1.0\%$ and 2.0% results in an increment of 4.85% and 9.79%, respectively.
- The results represent that using DF is more effective than $Fe_3O_4/H_2O FF$ in terms of THP .
- The highest average Nu is obtained in $B_0=0.5T DC MF$. However, the highest PEC is acquired in $B_0=0.3T DC MF$.
- When investigating the PEC results in applied $DC MF$, increments of 27.97%, 28.30%, 28.57%, and 28.31% are realized in $Fe_3O_4/H_2O FF$ flowing through DT exposed to $B_0=0.03T$, 0.05T, 0.3T, and 0.5T $DC MF$, respectively.
- Noteworthy and explicit visual results have been obtained in DF and MF effects.

CRediT author statement

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Kamil Arslan: Methodology, Writing - Review & Editing, Supervision, Project Administration.

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Addullah Dağdeviren: Visualization.

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